

Spin degeneracy in multi-hadron systems with a heavy quark

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Abstract

We study multi-hadron systems with a single heavy quark (charm or bottom) in the limit of heavy quark mass. We show that the spin degeneracy of the states with quantum numbers $(j + 1/2)^P$ and $(j - 1/2)^P$ for $j \neq 0$, known in a single hadron, can be generalized to multi-hadron systems. The spin degeneracy is the universal phenomena for any multi-hadron systems with a single heavy quark, irrespective of their internal structure, including compact multi-quarks, hadronic molecules and exotic nuclei. We demonstrate that the spin degeneracy is realized in the hadronic systems formed by a heavy hadron effective theory.

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Recent experimental developments in hadron spectroscopy have unveiled the existence of various exotic hadrons which are considered to have extraordinary structures. To analyze their properties is intimately related to the fundamental problems in QCD, such as color confinement and dynamical chiral symmetry breaking. Especially for charm and bottom flavors, there have been many experimental evidences for the existence of the exotic hadrons, such as X , Y and Z for charm sector and Y_b and Z_b for bottom sector [1]. Theoretically, not only exotic hadrons, but also exotic nuclei with charm and bottom are discussed. Those states can be explored experimentally at facilities, such as J-PARC, GSI-FAIR, RHIC and LHC [2]. Heavy exotic hadrons and nuclei will bring us a new insight from the quark dynamics to the nuclear dynamics, which cannot be accessed by light flavor hadrons. Although many model calculations have been extensively performed in the literature, it will be eagerly required to have the rigorous knowledge directly based on QCD.

A unique feature of charm and bottom quarks is that their masses are heavier than the energy scale of light quark QCD. In the heavy mass limit, it leads to the spin symmetry [3–7]. It has been known that, in a hadron with a single heavy quark, the spin of the heavy quark is decoupled from the total angular momentum of the light quarks and gluons, the “brown muck” which is everything other than the heavy quark in the hadron [8]. As a consequence, there appears a pair of degenerate states with total angular momentum and parity, $(j - 1/2)^P$ and $(j + 1/2)^P$, for $j \neq 0$, while a single state for $j = 0$, where j is the total angular momentum of the brown muck. The spin degeneracy has been addressed in the context of single hadrons, such as mesons and baryons including excited states [4–11]. The purpose of the present Letter is to apply the idea of the spin degeneracy to multi-hadron systems as exotic hadrons (irrespective of multi-quarks, hadronic molecules and exotic nuclei) containing a single heavy quark. We will discuss that the new structure exists in those systems, and find a universal nature in their mass spectroscopy which will provide us a basic information for both theoretical and experimental studies.

Let us consider a heavy quark Q with mass m_Q in QCD. Denoting the four velocity of the heavy quark as v^μ with $v^2 = 1$, we introduce the effective field $Q_v(x) = e^{im_Q v \cdot x} \frac{1+\not{v}}{2} Q(x)$ for the positive energy component of $Q(x)$. The effective Lagrangian in the $1/m_Q$ expansion is given by $\mathcal{L}_{\text{HQET}} = \bar{Q}_v v \cdot i D Q_v + \mathcal{O}(1/m_Q)$ with the covariant derivative D_μ . This is the Lagrangian in the heavy quark effective theory (HQET) [3–7]. A hadron with a single heavy quark is composed of the heavy quark with spin \vec{S} and the brown muck with total angular

momentum \vec{j} . The total angular momentum of the hadron is $\vec{J} = \vec{S} + \vec{j}$. In the limit of heavy quark mass ($m_Q \rightarrow \infty$), \vec{S} is a conserved quantity, because the spin flip terms are suppressed in the $1/m_Q$ expansion of $\mathcal{L}_{\text{HQET}}$. This is called the heavy quark spin symmetry. Clearly \vec{J} is conserved. Therefore, we find that \vec{j} is conserved, even though the brown muck is a highly non-perturbative object. Thus, we confirm that the spin degeneracy is realized as addressed previously.

Interestingly, the notion of the spin degeneracy is generally applied, not only to ground states and higher excited states, but also to multi-hadron systems and even to exotic nuclear systems, as far as the states contain a single heavy (anti)quark. Here we consider exotic hadrons with a single heavy antiquark, whose quark contents are minimally given by $\bar{Q}q^n$ ($n = 3B + 1$ with baryon number $B \geq 0$) with a heavy antiquark \bar{Q} and many light quarks q . We should note that the state is in fact a superposition of n light quarks plus any number of $q\bar{q}$ pairs and gluons g for a given quantum number;

$$\bar{Q} \underbrace{q \cdots q}_n + \bar{Q} \underbrace{q \cdots q}_{n-1} q \bar{q} + \bar{Q} \underbrace{q \cdots q}_{n-2} q \bar{q} g + \cdots. \quad (1)$$

Then, we ask the question whether the exotic hadrons have the spin degeneracy as normal hadrons. In those systems, the heavy quark spin for \bar{Q} is a conserved quantity in the heavy mass limit, and the total angular momentum is also conserved. Therefore, the total angular momentum of the ensemble of the light components, $q \cdots q + q \cdots q \bar{q} + q \cdots q \bar{q} g + \cdots$, in Eq. (1) is also conserved. Consequently, we obtain the result that there is a pair of degenerate states with $(j - 1/2)^P$ and $(j + 1/2)^P$ for $j \neq 0$, and a single state for $j = 0$, where j^P is the total angular momentum and parity of the light components ($P = -P$).

In the present discussion, we call the light components in Eq. (1) “light spin-complex” (or “spin-complex” in short). The reason of introducing the new term is explained. When the state is a compact multi-quark, the spin-complex is an ensemble of light quarks and gluons. This is a simple generalization of the brown muck in a single hadron. When the state is a spatially extended hadronic molecule, however, the state can be composed of hadrons and the $\bar{Q}q$ meson. Then, the spin-complex is a composite system with hadrons and a light quark q from the $\bar{Q}q$ meson. This is the reason why we use “complex”, meaning not only quarks and gluons (brown muck), but also a complex of quarks, gluons and hadrons. As a typical configuration, it can be $q\bar{q}$ mesons and a light quark q for $B = 0$, or qqq baryons and

a light quark q for $B \geq 1$. The latter can be applied to the exotic nuclei containing the $\bar{Q}q$ meson.

The spin-complex is a new object in exotic hadrons, which has not been addressed in the literature. Note that the spin-complex is not a colorless (singlet) object, but a colorful (triplet) object like the brown muck. How the spin-complex is formed (as a compact multi-quark or a composite state) is a highly nonperturbative problem in QCD. Nevertheless, the spin-complex is an object with a good quantum number j^P . Therefore, the spin degeneracy for $j \neq 0$ and no degeneracy for $j = 0$ is a universal phenomena regardless whether the state is a compact multi-quark state, an extended hadronic molecule state or even a mixture of them.

We conclude from QCD that the spin degeneracy occurs in any multi-hadron systems with a single heavy quark, as far as the heavy quark limit is taken. Because of the universal nature, the spin degeneracy in the multi-hadron systems should be seen for hadronic molecules described by the low-energy effective theory based on the heavy quark symmetry from QCD, where the fundamental degrees of freedom are hadrons. This subject will be investigated in the following.

Now, let us discuss hadronic molecules with flavor exotic compound by a heavy meson $P^{(*)} \sim \bar{Q}q$ and a nucleon N . We denote the heavy meson with $J^P = 0^-$ (1^-) as P (P^*), and $P^{(*)}$ stands for one of the heavy meson doublet (P, P^*). We study whether the $P^{(*)}N$ systems exhibit the spin degeneracy.

To demonstrate concretely, we consider the one pion exchange potential between $P^{(*)}$ and N in Refs. [12, 13]. The heavy quark symmetry is realized in the degenerate masses of P and P^* and the common couplings of πPP^* and πP^*P^* vertices. We will investigate the states with $1/2^-$ and $3/2^-$ in detail, and later will extend the discussion to general cases of $(j - 1/2)^P$ and $(j + 1/2)^P$.

The wave function in $P^{(*)}N$ has multi-channels; $\{|PN(^2S_{1/2})\rangle, |P^*N(^2S_{1/2})\rangle, |P^*N(^4D_{1/2})\rangle\}$ for $1/2^-$, $\{|PN(^2D_{3/2})\rangle, |P^*N(^4S_{3/2})\rangle, |P^*N(^4D_{3/2})\rangle, |P^*N(^2D_{3/2})\rangle\}$ for $3/2^-$. Then, the Hamiltonians are given by

$$H_{1/2^-} = \begin{pmatrix} K_0 & \sqrt{3}C & -\sqrt{6}T \\ \sqrt{3}C & K_0 - 2C & -\sqrt{2}T \\ -\sqrt{6}T & -\sqrt{2}T & K_2 + (C - 2T) \end{pmatrix},$$

$$H_{3/2^-} = \begin{pmatrix} K_2 & \sqrt{3}T & -\sqrt{3}T & \sqrt{3}C \\ \sqrt{3}T & K_0 + C & 2T & T \\ -\sqrt{3}T & 2T & K_2 + C & -T \\ \sqrt{3}C & T & -T & K_2 - 2C \end{pmatrix},$$

for $1/2^-$ and $3/2^-$, respectively. We define the kinetic term $K_\ell = -(\partial^2/\partial r^2 + (2/r)\partial/\partial r - \ell(\ell+1)/r^2)/2\mu$ for angular momentum ℓ , and the reduced mass μ coincides with the mass of the nucleon m_N in the limit of infinite mass of $P^{(*)}$. We also define $C = \kappa C(r; m_\pi)$ and $T = \kappa T(r; m_\pi)$, with $\kappa = (g_\pi g_{\pi NN}/\sqrt{2}m_N f_\pi)(\vec{\tau}_P \cdot \vec{\tau}_N/3)$ with a $P^{(*)}P^*\pi$ ($NN\pi$) coupling constant g_π ($g_{\pi NN}$), the pion decay constant f_π , and isospin matrices $\vec{\tau}_P$ and $\vec{\tau}_N$ for $P^{(*)}$ and N , respectively, and the central potential $C(r; m_\pi)$ and the tensor potential $T(r; m_\pi)$ (r the distance between $P^{(*)}$ and N , and m_π the pion mass) whose explicit forms are given in Refs. [12, 13]. The PN and P^*N states can be mixed, and the states with different angular momenta can also be mixed. The former originates in the heavy quark spin symmetry, and the latter does in the tensor force of the pion exchange potential.

Previously we mentioned the existence of the spin-complex in the multi-hadron systems. We then ask what the spin-complex in the present $P^{(*)}N$ system is. We remember that the $P^{(*)}N$ molecule state is composed of the meson $P^{(*)} \sim \bar{Q}q$ and a nucleon N . In view of the heavy quark spin symmetry, this system is decomposed into the heavy antiquark \bar{Q} and the remaining light degrees of freedom, namely the spin-complex. In our model space, the spin-complex is given by Nq from the nucleon N and the light quark q in $P^{(*)}$. Combined with the heavy antiquark \bar{Q} , the basis states can be written as $\{|[Nq]_{0+}^{(0,S)}\bar{Q}\rangle_{1/2^-}, |[Nq]_{1+}^{(1,S)}\bar{Q}\rangle_{1/2^-}, |[Nq]_{1+}^{(1,D)}\bar{Q}\rangle_{1/2^-}\}$ and $\{|[Nq]_{1+}^{(1,S)}\bar{Q}\rangle_{3/2^-}, |[Nq]_{1+}^{(1,D)}\bar{Q}\rangle_{3/2^-}, |[Nq]_{2+}^{(0,D)}\bar{Q}\rangle_{3/2^-}, |[Nq]_{2+}^{(1,D)}\bar{Q}\rangle_{3/2^-}\}$, respectively, for $1/2^-$ and $3/2^-$. Here $[Nq]_{j^P}^{(S,L)}$ denotes the spin-complex composed of a nucleon and a quark (in $P^{(*)}$ meson) with total spin S , angular momentum L , and total angular momentum and parity j^P . The particle basis by $\{|P^{(*)}N(^{2S+1}L_J)\rangle\}$ and the spin-complex basis by $\{|[Nq]_{j^P}^{(S,L)}\bar{Q}\rangle_{JP}\}$ are related by unitary matrix, U for $1/2^-$ and U' for $3/2^-$, and the Hamiltonians $H_{1/2^-}$ and $H_{3/2^-}$ are transformed as,

$$U^{-1}H_{1/2^-}U$$

$$\begin{aligned}
&= \left(\begin{array}{c|cc} K_0-3C & 0 & 0 \\ \hline 0 & K_0+C & -2\sqrt{2}T \\ 0 & -2\sqrt{2}T & K_2+(C-2T) \end{array} \right), \\
&U'^{-1}H_{3/2^-}U' \\
&= \left(\begin{array}{cc|cc} K_0+C & 2\sqrt{2}T & 0 & 0 \\ 2\sqrt{2}T & K_2+(C-2T) & 0 & 0 \\ \hline 0 & 0 & K_2-3C & 0 \\ 0 & 0 & 0 & K_2+(C+2T) \end{array} \right).
\end{aligned}$$

Thus, with the spin-complex basis, we obtain the block-diagonal forms, $U^{-1}H_{1/2^-}U = \text{diag}(H_{1/2^-}^{(0+)}, H_{1/2^-}^{(1+)})$ and $U'^{-1}H_{3/2^-}U' = \text{diag}(H_{3/2^-}^{(1+)}, H_{3/2^-}^{(2+)})$, with the notation $H_{JP}^{(j^P)}$ for the J^P state containing the spin-complex with j^P . The off-diagonal terms in $H_{3/2^-}^{(2+)}$ vanish because the one pion exchange potential is used. When other interactions are employed, the off-diagonal terms in $H_{JP}^{(j^P)}$ may exist in general. In our model space, we consider only Nq for the spin-complex. Even when the other components such as Δq , $N\pi q$ are considered, the Hamiltonians are block-diagonalized with the spin-complex basis, as far as the heavy quark symmetry is taken.

Importantly, we note that $H_{1/2^-}^{(1+)}$ coincides with $H_{3/2^-}^{(1+)}$ except for the irrelevant sign of the off-diagonal terms. Therefore, $H_{1/2^-}^{(1+)}$ and $H_{3/2^-}^{(1+)}$ have exactly the same eigenvalues and eigenstates. For bound states, this is truly the spin degeneracy for $P^{(*)}N$ with $1/2^-$ and $3/2^-$, because the spin-complex with 1^+ is commonly contained in $1/2^-$ and $3/2^-$ states. For scattering states, the equivalence is also seen with the spin-complex basis. The state described by $H_{1/2^-}^{(0+)}$ is the single state containing the spin-complex with 0^+ . The block-diagonalization of Hamiltonians is possible also for higher spin states. For example, $H_{3/2^-}^{(2+)}$ and $H_{5/2^-}^{(2+)}$ form a degenerate pair of $3/2^-$ and $5/2^-$ containing the common spin-complex with 2^+ .

The eigenstates of $H_{1/2^-}^{(1+)}$ and $H_{3/2^-}^{(1+)}$ are the linear combinations as $\cos\theta|[Nq]_{1^+}^{(1,S)}\bar{Q}\rangle_{1/2^-} + \sin\theta|[Nq]_{1^+}^{(1,D)}\bar{Q}\rangle_{1/2^-}$ and $\cos\theta|[Nq]_{1^+}^{(1,S)}\bar{Q}\rangle_{3/2^-} + \sin\theta|[Nq]_{1^+}^{(1,D)}\bar{Q}\rangle_{3/2^-}$, respectively. Although the mixing angle θ is determined by the interaction among the light degrees of freedom, the same mixing angle for $1/2^-$ and $3/2^-$ is required from the heavy quark symmetry. This means that the fraction of each component in the particle basis is uniquely determined. The fraction is related to decay and production rates in weak, electromagnetic and strong

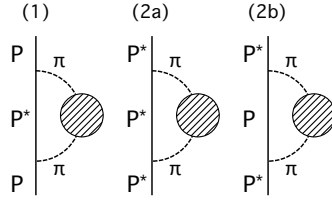


FIG. 1. The diagrams of the self-energies for (1) P meson and (2a,b) P^* meson in the nuclear matter. The solid (dashed) lines are for $P^{(*)}$ (pions). See the text for details.

processes.

We can similarly discuss the spin degeneracy for any pair of states with $(j - 1/2)^P$ and $(j + 1/2)^P$ for $j \neq 0$, which contain the spin-complex with $j^{\mathcal{P}}$ ($\mathcal{P} = -P$) in common. The Hamiltonians of the $(j - 1/2)^P$ and $(j + 1/2)^P$ states are the same; $H_{(j-1/2)^P}^{(j^{\mathcal{P}})} = H_{(j+1/2)^P}^{(j^{\mathcal{P}})}$. For higher $j \pm 1/2$, there can be resonant states. The spin degeneracy occurs, not only for the bound states, but also for the resonant states.

The result for the spin degeneracy in the hadronic molecules with baryon number one will be applied to exotic nuclei with arbitrary baryon number, which contain a single heavy quark. As a limiting case, we consider the uniform nuclear matter with a single $P^{(*)} \sim \bar{Q}q$ meson. Note that the ground state is the nuclear matter, not vacuum. When the $P^{(*)}$ meson exists in the nuclear matter (e.g. see Ref. [14] and the references therein for $\bar{D}^{(*)}$ ($B^{(*)}$) meson), the $P^{(*)}$ meson interacts with the neighboring nucleons, and the spin-complex may contain $NN^{-1}q + NNN^{-1}N^{-1}q + \dots$ with the particle (nucleon) N , the hole N^{-1} and the light quark q from $P^{(*)}$. Because the spin of the \bar{Q} quark is irrelevant to the structure of the spin-complex, it should lead to the spin degeneracy, namely the degeneracy of the self-energies of P and P^* in the nuclear matter.

Let us discuss the self-energy of the $P^{(*)}$ meson in the nuclear matter, given by the diagrams in Fig. 1. We perform the perturbative analysis at $\mathcal{O}(g_\pi^2)$. We introduce the pion self-energy $-i\Pi_\pi^{ab}(k)$ in the nuclear matter with the pion momentum k and the final (initial) isospin a (b), as shown by the blobs. Indeed, it stands for the creation of many pairs of particle and hole, $NN^{-1} + NNN^{-1}N^{-1} + \dots$, which contribute to the spin-complex. In the heavy mass

limit, the self-energies of P and P^* are given, respectively, as

$$-i\Sigma_P = \int \frac{d^4k}{(2\pi)^4} \frac{k^2 - (v \cdot k)^2}{2v \cdot (-k) + i\epsilon} \left(\frac{1}{k^2 - m_\pi^2 + i\epsilon} \right)^2 \eta(k),$$

with $\eta(k) = -\left(2g_\pi/\sqrt{2}f_\pi\right)^2 \tau^a \Pi_\pi^{ab}(k) \tau^b$ for P in Fig. 1(1), and $-i\Sigma_{P^*} = -i\Sigma_{P^*}^{(P^*)} - i\Sigma_{P^*}^{(P)}$ with $\Sigma_{P^*}^{(P^*)} = (2/3)\Sigma_P$ and $\Sigma_{P^*}^{(P)} = (1/3)\Sigma_P$ for P^* in Fig. 1(2a,b). Here v^μ is the four velocity for $P^{(*)}$, and ϵ is an infinitely small positive number. The factor in the numerator in the first term of the integrand results from the spin structure of the $P^{(*)}$ mesons. We note that, thanks to the heavy quark spin symmetry (i.e. the same coupling strengths for the $PP^*\pi$ and $P^*P^*\pi$ vertices and the large mass limit for P and P^*), the contributions from (1) and (2a,b) in Fig. 1 are the same except for the overall coefficients. Their fraction 3 : 2 : 1 is understood intuitively from the counting of the spin degrees of freedom in the intermediate states. Consequently, we find that the self-energy of the P meson is equal to that of the P^* meson; $-i\Sigma_P = -i\Sigma_{P^*}$. We confirm that the result in Ref. [14], where the pion self-energy was calculated at one-loop order, is consistent with the present conclusion, when the limit of heavy quark mass is taken. The spin degeneracy of P and P^* in the nuclear matter is consistent with the discussion from QCD. It will be naturally expected that the spin degeneracy will hold for any higher order of g_π as well as for any excited pairs of particle and hole [15].

So far we have concentrated on a heavy *antiquark*. A similar discussion will be applied to the multi-hadron systems with a heavy quark Q , whose quark contents are given by $Q\bar{q}$ or Qq^n ($n = 3B - 1$ with baryon number $B \geq 1$). The spin degeneracy of $(j \pm 1/2)^P$ states for $j \neq 0$ and no degeneracy for $j = 0$ should hold for any states. In the literature, the DN ($\bar{B}N$) [16] and $\Lambda_c N$ [17] systems for the hadronic molecules as well as the DNN systems [18] and the nuclear matter with a D meson [19] for the exotic nuclei are discussed. Once again, in the limit of heavy quark mass, the bound states as well as resonant states should exhibit the spin degeneracy.

The concept of spin-complex for multi-hadron systems brings us a new insight for the constituents of hadrons. In some models in the low energy QCD, the fundamental degrees of freedom are considered to be quarks in the constituent quark model, and hadrons in a hadronic molecule model. However, the heavy quark spin symmetry tells us an importance to decompose the spin of the heavy quark and the total angular momentum of the other light degrees of freedom. This is a new way to look especially at exotic hadrons and nuclei

with a single heavy quark. The spin degeneracy induced from the existence of the spin-complex will give a guidance for experimental search of the exotic hadrons and nuclei with a single charm or bottom quark. In the real world, however, the breaking of the heavy quark symmetry violates the strict spin degeneracy. Nevertheless, the spin-complex is useful to both theoretical and experimental analyses. The extrapolation from charm and bottom will enable us to reach the information in the heavy quark limit. When one state is observed, the partner state can also be found nearby. Furthermore the structure of the spin-complex will be studied through the decay and production rates.

In summary, we consider multi-hadron systems with a single heavy quark in the limit of heavy quark mass. The spin degeneracy is a universal phenomena of QCD for the multi-hadrons with a single heavy (anti)quark, regardless whether the systems are the compact multi-quark states or the extended hadronic molecule states or the mixture of them. We also show explicitly based on the heavy hadron effective theory that the spin degeneracy is realized for the $P^{(*)}N$ hadronic molecule systems and the $P^{(*)}$ meson in the nuclear matter. We propose the existence of the spin-complex as a new object in the multi-hadron systems. The notion of the spin-complex may be applied further in the deconfinement phases, such as the quark-gluon plasma, the color superconductivity and the quarkyonic matter [20]. The spin degeneracy will give us a guiding principle for analysis of multi-hadron systems with a single heavy quark.

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